

# An Overview of Machine Teaching

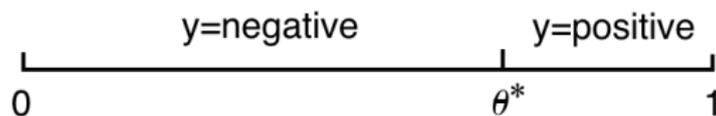
Adish Singla, Jerry Zhu

NIPS 2017 Workshop on  
Teaching Machines, Robots, and Humans

## A prototypical machine teaching task

# Compare passive learning, active learning, teaching

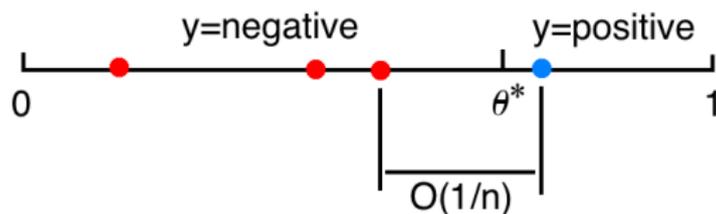
Example: learn a 1D threshold classifier



# Passive learning

$$x_1, \dots, x_n \sim U[0, 1]$$

$$y_i = \theta^*(x_i)$$



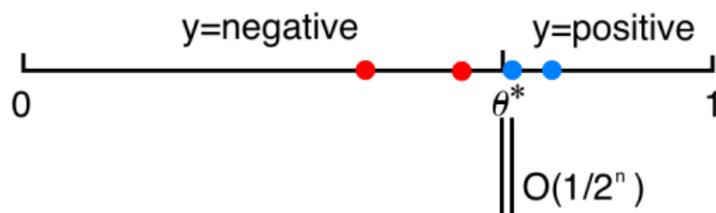
With large probability

$$|\hat{\theta} - \theta^*| = O(n^{-1}) \leq \epsilon$$

$$n \geq O(\epsilon^{-1})$$

# Active learning

- ▶ learner picks query  $x$ , oracle answers  $y = \theta^*(x)$
- ▶ binary search

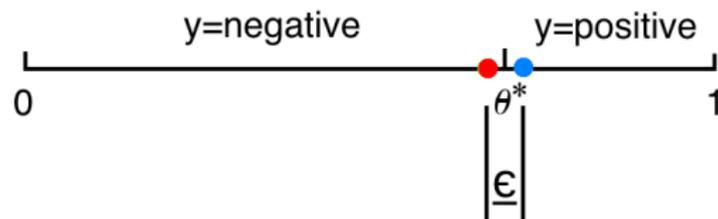


$$|\hat{\theta} - \theta^*| = O(2^{-n}) \leq \epsilon$$

$$n \geq O(\log(\epsilon^{-1}))$$

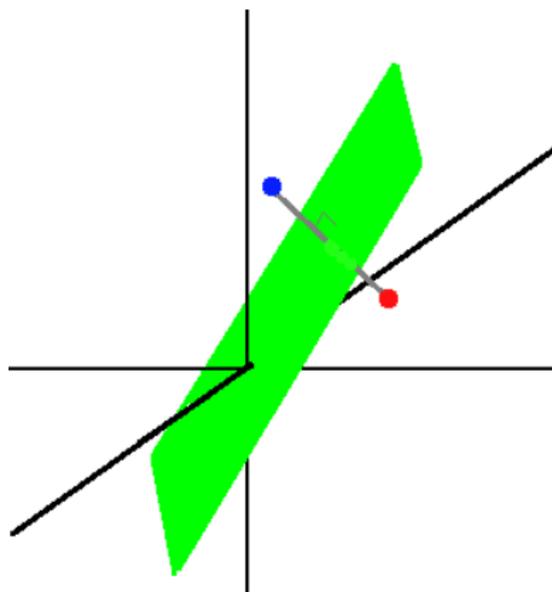
# Machine teaching

- ▶ teacher can design an optimal training set of size 2



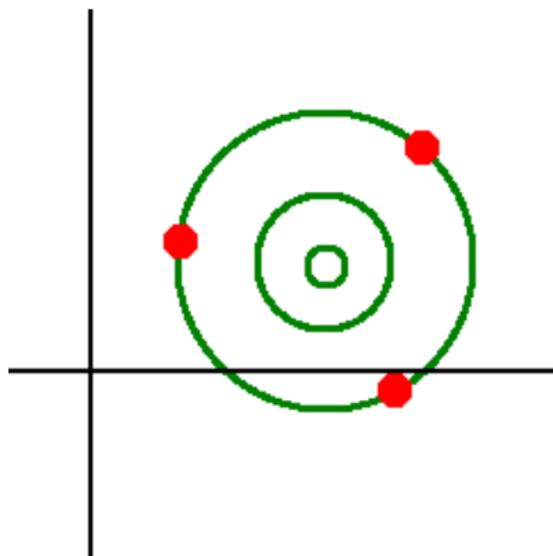
$$n = 2, \forall \epsilon > 0$$

## Another example: teach hard margin SVM



Remark: Teaching Dimension  $TD = 2$  but  $VC = d + 1$

## Yet another example: teach Gaussian density



$TD = d + 1$ : tetrahedron vertices

# Machine learning vs. machine teaching

Machine learning ( $D$  given, learn  $\theta$ )

$$\min_{\theta} \sum_{(x,y) \in D} \ell(x, y, \theta) + \lambda \|\theta\|^2$$

Machine teaching ( $\theta^*$  given, learn  $D$ )

$$\begin{aligned} \min_{D, \hat{\theta}} \quad & \|\hat{\theta} - \theta^*\|^2 + \eta \|D\|_0 \\ \text{s.t.} \quad & \hat{\theta} = \operatorname{argmin}_{\theta} \sum_{(x,y) \in D} \ell(x, y, \theta) + \lambda \|\theta\|^2 \end{aligned}$$

$D$  usually not *i.i.d.*

# Why bother if we already know $\theta^*$ ?

- ▶ education
- ▶ adversarial attacks
- ▶ ...

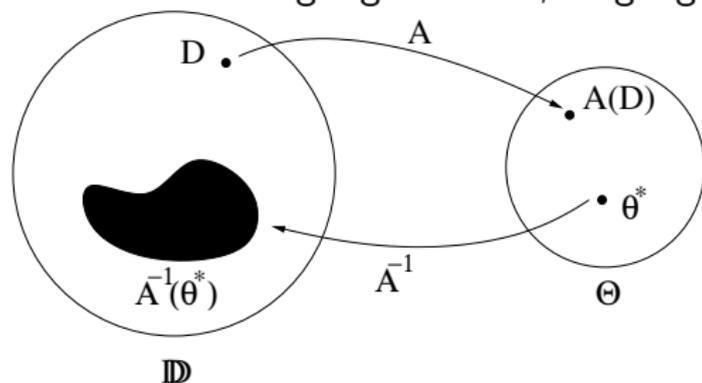
# Machine teaching generic form

$$\begin{aligned} \min_{D, \hat{\theta}} \quad & \text{TeachingRisk}(\hat{\theta}) + \eta \text{TeachingCost}(D) \\ \text{s.t.} \quad & \hat{\theta} = \text{MachineLearning}(D) \end{aligned}$$

- ▶ exact vs. approximate teaching
- ▶ parameter vs. generalization error
- ▶ cost not always number of items
- ▶ any of the constraint forms

# The coding view

message= $\theta^*$ , decoder=learning algorithm  $A$ , language= $\mathbb{D}$



## In other words

teach·ing

/'teCHiNG/

*noun*

1. controlling
2. shaping
3. persuasion
4. influence maximization
5. attacking
6. poisoning

## Characterizing the space of teaching tasks

# The friend vs. foe dimension

## friend

- ▶ education
- ▶ improving cognitive models
- ▶ fast classifier training
- ▶ debugging machine learners
- ▶ ...
- ▶ training-set poisoning attacks (not test-time adversarial attacks)

## foe

# The human vs. machine dimension

- ▶ machine teacher, machine learner: attacks
- ▶ machine teacher, human learner: education
- ▶ human teacher, machine learner: fast classifier training
- ▶ human teacher, human learner: (not this workshop)

# The batch vs. sequential dimension

## Batch teaching

- ▶ batch learners

## Sequential teaching

- ▶ stochastic gradient descent learner
- ▶ multiarmed bandits
- ▶ reinforcement learning (e.g. teaching by demonstration)

# The learner anticipation dimension

- ▶ does not anticipate teaching (standard learners)
  - ▶ version space learner  $\{\theta \text{ agrees with } D\}$
  - ▶ Bayesian learner  $p(\theta \mid D)$
  - ▶ convex regularized empirical risk minimizer

$$\min_{\theta} \sum_{(x,y) \in D} \ell(x, y, \theta) + \lambda \|\theta\|^2$$

- ▶ deep neural network
  - ▶ cognitive model
- ▶ anticipates teaching
  - ▶ especially when human is involved

# The learner anticipation dimension (cont.)

A smart learner can

- ▶ educate the (suboptimal human) teacher in the structure of the optimal teaching set
- ▶ detect suboptimal teaching and switch to active learning
- ▶ translate the teaching set aimed at a different learner

Recursive teaching dimension *RTD* (vs. classical *TD*)

# The learner transparency dimension

## clearbox

- ▶ bilevel optimization

$$\begin{aligned} \min_{D, \hat{\theta}} \quad & \text{TeachingRisk}(\hat{\theta}) + \eta \text{TeachingCost}(D) \\ \text{s.t.} \quad & \hat{\theta} = \text{MachineLearning}(D) \end{aligned}$$

- ▶ ...
- ▶ some learning hyper-parameters unknown. Probe and teach
- ▶ ...
- ▶ evaluation function on  $D$ . Bayesian optimization.

## blackbox

# The number of learners dimension

- ▶ one lecture, one student (standard)
- ▶ one lecture, many students
  - ▶ worst-case guarantee: minimax risk
  - ▶ average-case guarantee: Bayes risk

# The “what’s in your training set” dimension

Items in  $D$  can be:

- ▶ pool-based teaching: subset (multiset) of a given pool  $\{(x_i, y_i)\}_{1:N}$
- ▶ synthetic / constructive teaching:
  - ▶ honest:  $x \in \mathcal{X}, y = \theta^*(x)$
  - ▶ liar:  $(x, y) \in \mathcal{X} \times \mathcal{Y}$ ; fake rewards. Ethics questions
- ▶ alter existing training set  $D_0 + (\delta_x, \delta_y)$
- ▶ features, pairwise comparisons (requires corresponding learner)

# The theory vs. empirical dimension

- ▶ teaching dimension  $TD$ , recursive teaching dimension  $RTD$ , preference-based  $TD$ , etc.

$$TD(\theta^*) \equiv \min_D \quad \|D\|_0$$

s.t.  $\{\theta^*\} = \text{VersionSpace}(D).$

- ▶ ...
- ▶ improve student test scores

## A few open problems

# Information complexity of teaching and learning

- ▶ relationship between recursive teaching dimension ( $RTD$ ) and VC-dimension ( $VCD$ )
  - ▶  $RTD$  is upper bounded by  $O(VCD)$ ?
- ▶ connections between above question and the long-standing open “sample compression conjecture” [Littlestone and Warmuth, 1986]

# New notions of teaching dimension (TD)

- ▶ complexity of teaching with new signals
  - ▶ e.g. features, pairwise comparison queries
- ▶ complexity of teaching with additional constraints
  - ▶ e.g. interpretable signals

# Solving the combinatorial, bilevel optimization problem

- ▶ bilevel optimization

$$\begin{aligned} \min_{D, \hat{\theta}} \quad & \text{TeachingRisk}(\hat{\theta}) + \eta \text{TeachingCost}(D) \\ \text{s.t.} \quad & \hat{\theta} = \text{MachineLearning}(D) \end{aligned}$$

- ▶ mixed integer nonlinear programming
  - ▶ even simple instances are NP-Hard (e.g. set-cover, subset sum)
- ▶ requires new approximation algorithms
  - ▶ e.g. via characterizing submodularity properties of the problem

# Machine teaching for reinforcement learning

- ▶ optimal demonstrations for inverse reinforcement learning
- ▶ teaching humans how to teach robots

# The need for a good cognitive model

- ▶ model-based vs. model-free approaches
  - ▶ 3 workshop papers on spaced repetition technique
- ▶ can machine teaching guide the search for better models?

# Novel applications and industry insights

- ▶ machine teaching for debugging machine learning?
- ▶ program synthesis, social robotics, etc.

## Workshop preview

# Cluster 1: Teacher who optimizes training data

## Posters:

- 3 Optimizing Human Learning
- 5 Interpretable Machine Teaching via Feature Feedback
- 7 Interpretable and Pedagogical Examples
- 11 Accelerating Human Learning with Deep Reinforcement Learning
- 12 Program2Tutor: Combining Automatic Curriculum Generation with Multi-Armed Bandits for Intelligent Tutoring Systems
- 15 Predicting Recall Probability to Adaptively Prioritize Study

## Talks:

- ▶ Emma Brunskill
- ▶ Burr Settles
- ▶ Le Song

## Cluster 2: Student who appreciates teaching

Posters:

- 2 Machine Education - The Way Forward for Achieving Trust-Enabled Machine Agents
- 4 Model Distillation with Knowledge Transfer from Face Classification to Alignment and Verification
- 6 Pedagogical Learning
- 13 Generative Knowledge Distillation for General Purpose Function Compression
- 14 Explainable Artificial Intelligence via Bayesian Teaching

## Cluster 3: Related Topics

### Posters:

- 1 Generative Adversarial Active Learning
- 8 Faster Reinforcement Learning Using Active Simulators
- 9 Gradual Tuning: A Better Way of Fine Tuning the Parameters of a Deep Neural Network
- 10 Machine Teaching: A New Paradigm for Building Machine Learning Systems

### Talks:

- ▶ Shay Moran
- ▶ Patrice Simard